

# Chapter 27

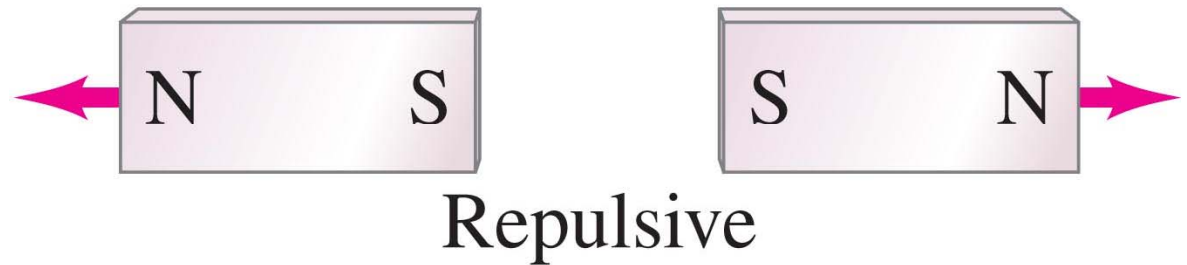
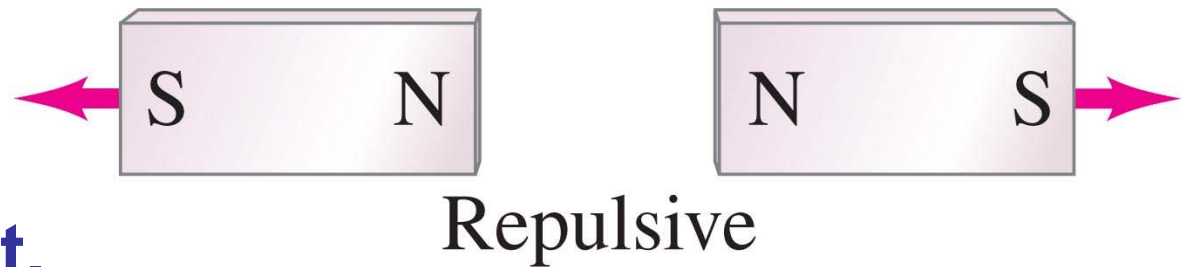
# Magnetism



# 27-1 Magnets and Magnetic Fields

Magnets have two ends – poles – called north and south.

Like poles repel;  
unlike poles attract.



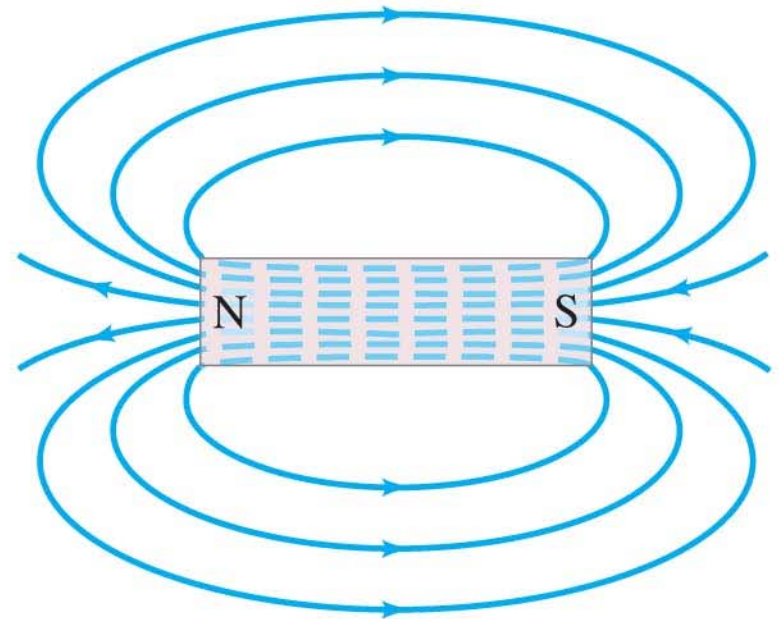
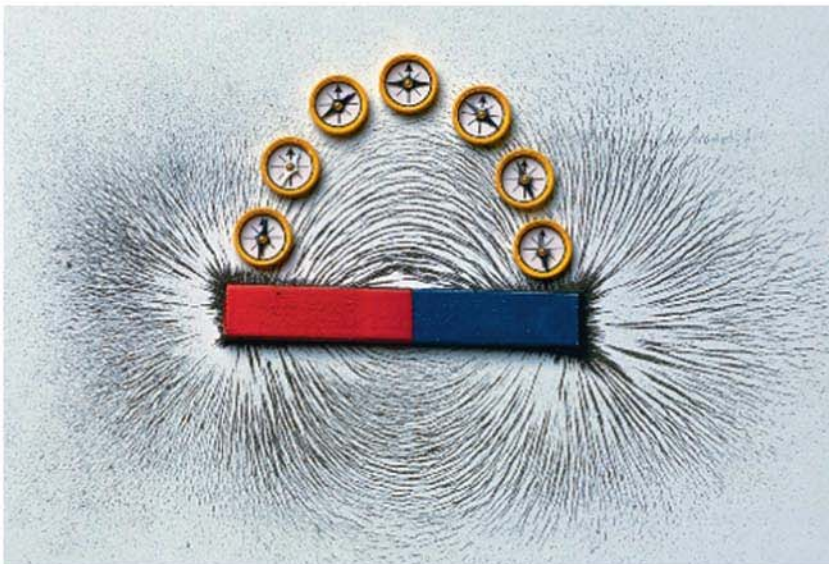
# 27-1 Magnets and Magnetic Fields

However, if you cut a magnet in half, you don't get a north pole and a south pole – you get two smaller magnets.



# 27-1 Magnets and Magnetic Fields

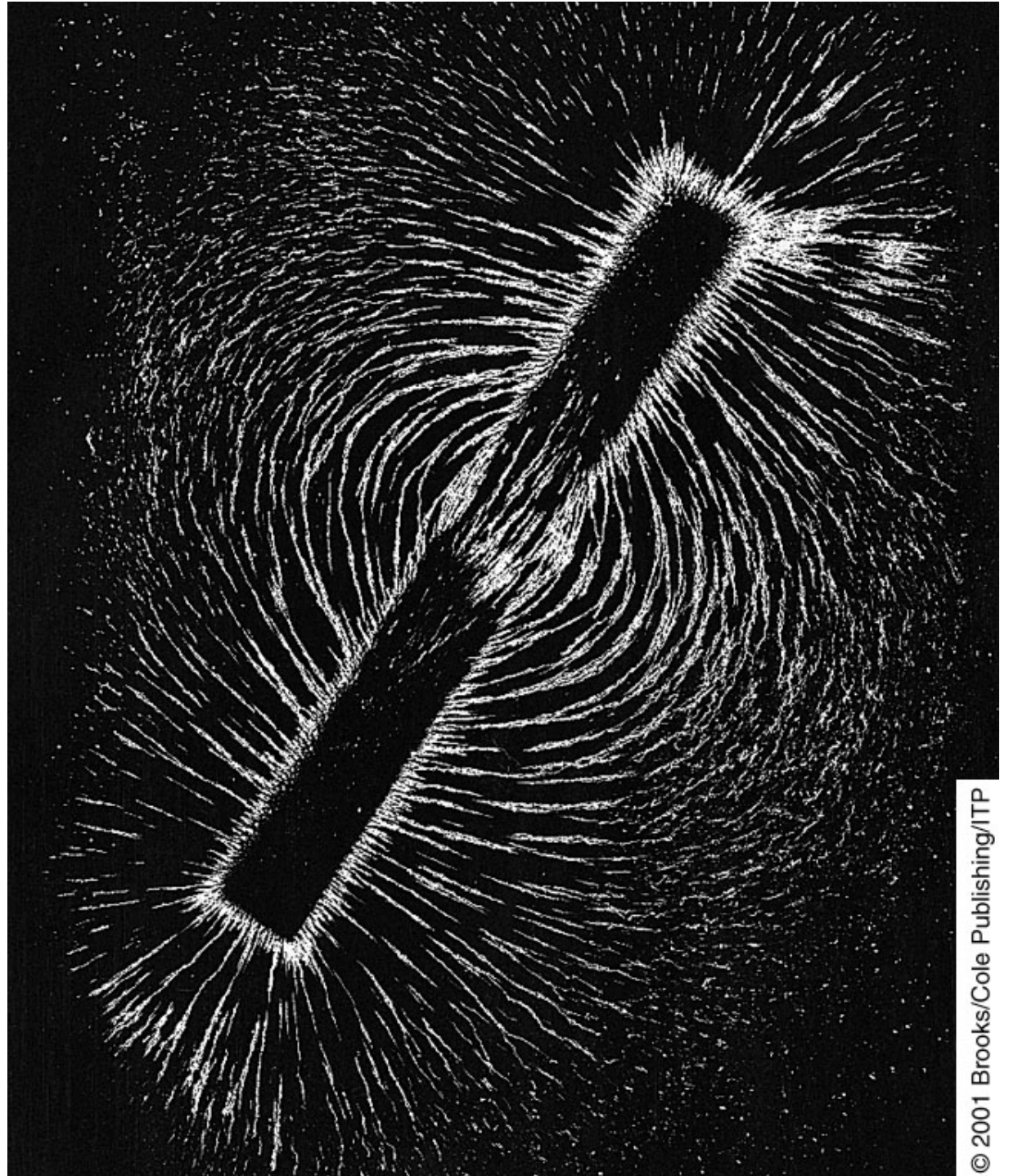
Magnetic fields can be visualized using magnetic field lines, which are always closed loops.



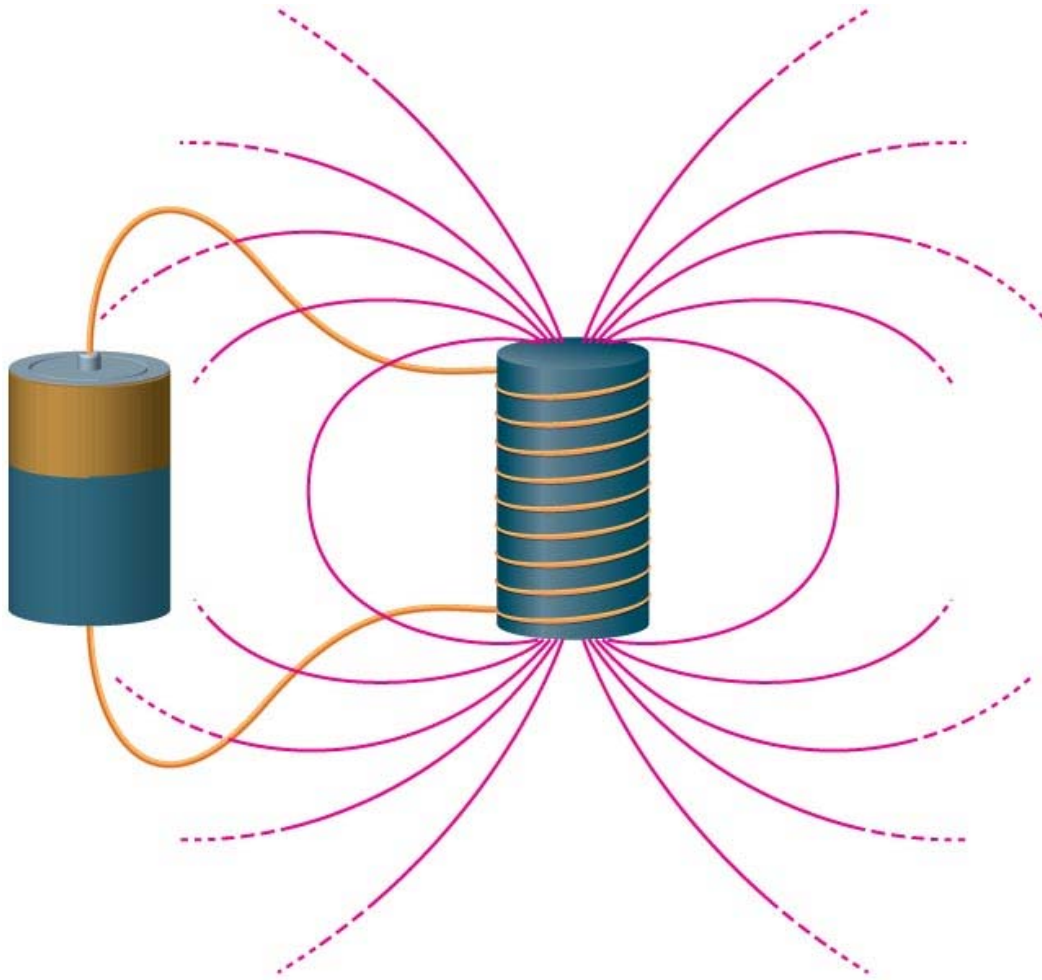
**Magnetism  
Plays a Major Role  
On the structure of the  
Sun  
and important on Earth  
Here Iron filings are  
Sprinkled about a  
Magnet and  
We get a sense of what  
Is happening  
Around the space of  
The magnet**

**FILM: MAGNET  
AND IRON FILINGS**

**FILM 3D FIELD**



# Sources of Magnetic Fields

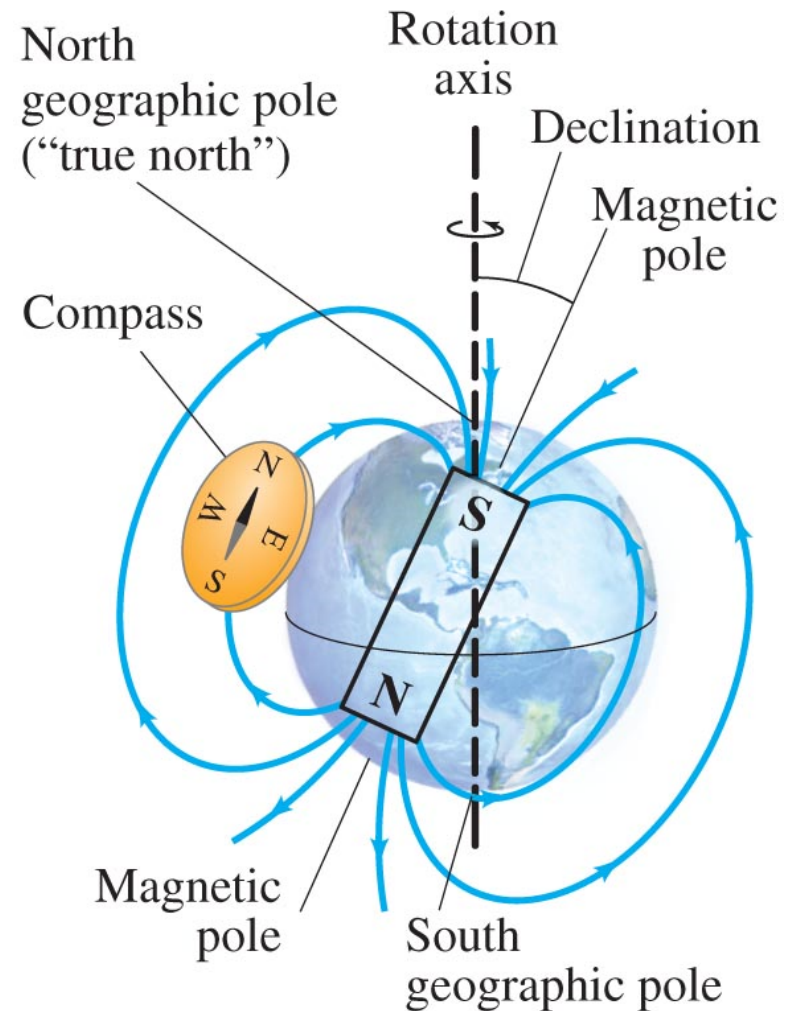


- Motions of charged particles are what create magnetic fields
- In Planets and the Sun and in devices!
- We use this for many applications

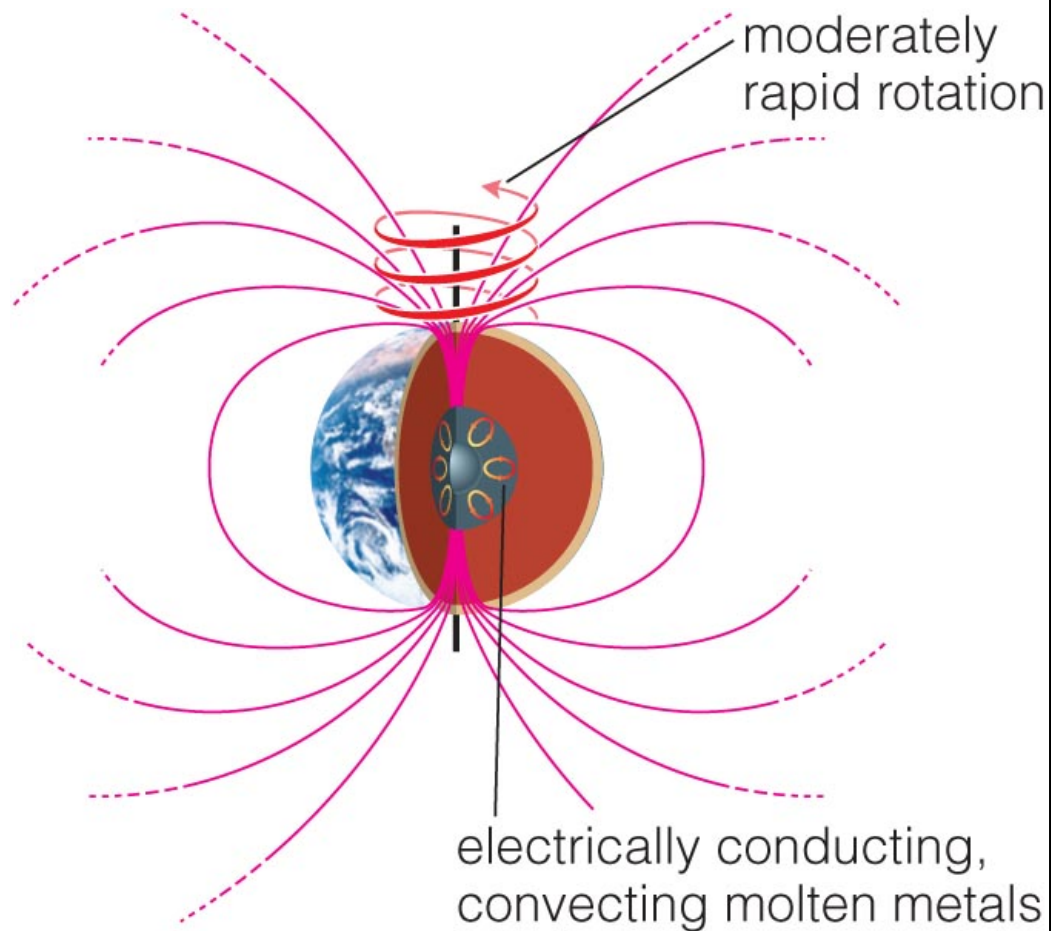
# 27-1 Magnets and Magnetic Fields

The Earth's magnetic field is similar to that of a bar magnet.

Note that the Earth's "North Pole" is really a south magnetic pole, as the north ends of magnets are attracted to it.



# Sources of Magnetic Fields



- A planet can have a magnetic field if charged particles are moving inside
- 3 requirements:
  - Molten interior
  - Convection
  - Moderately rapid rotation



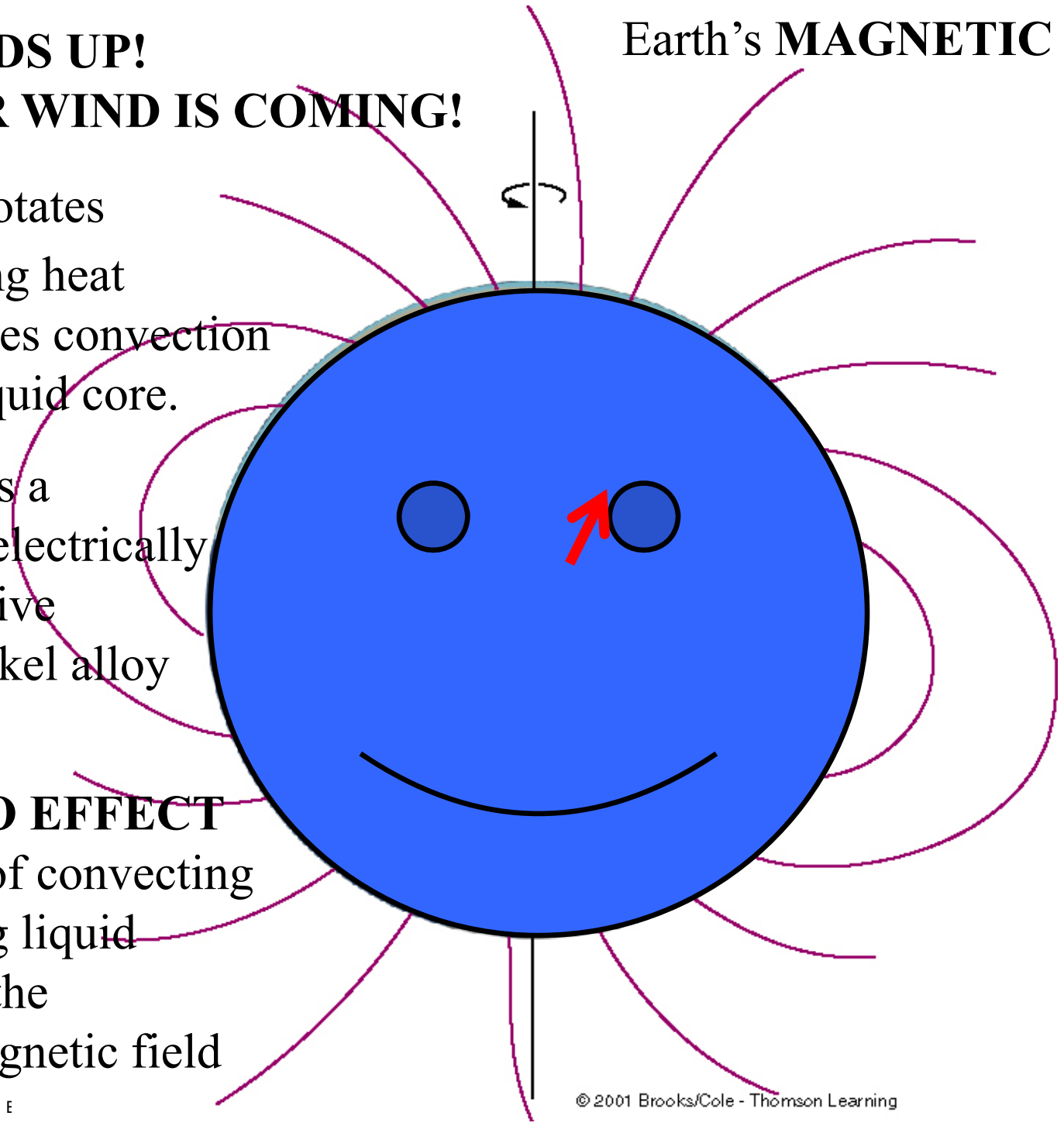
**SHIELDS UP!  
SOLAR WIND IS COMING!**

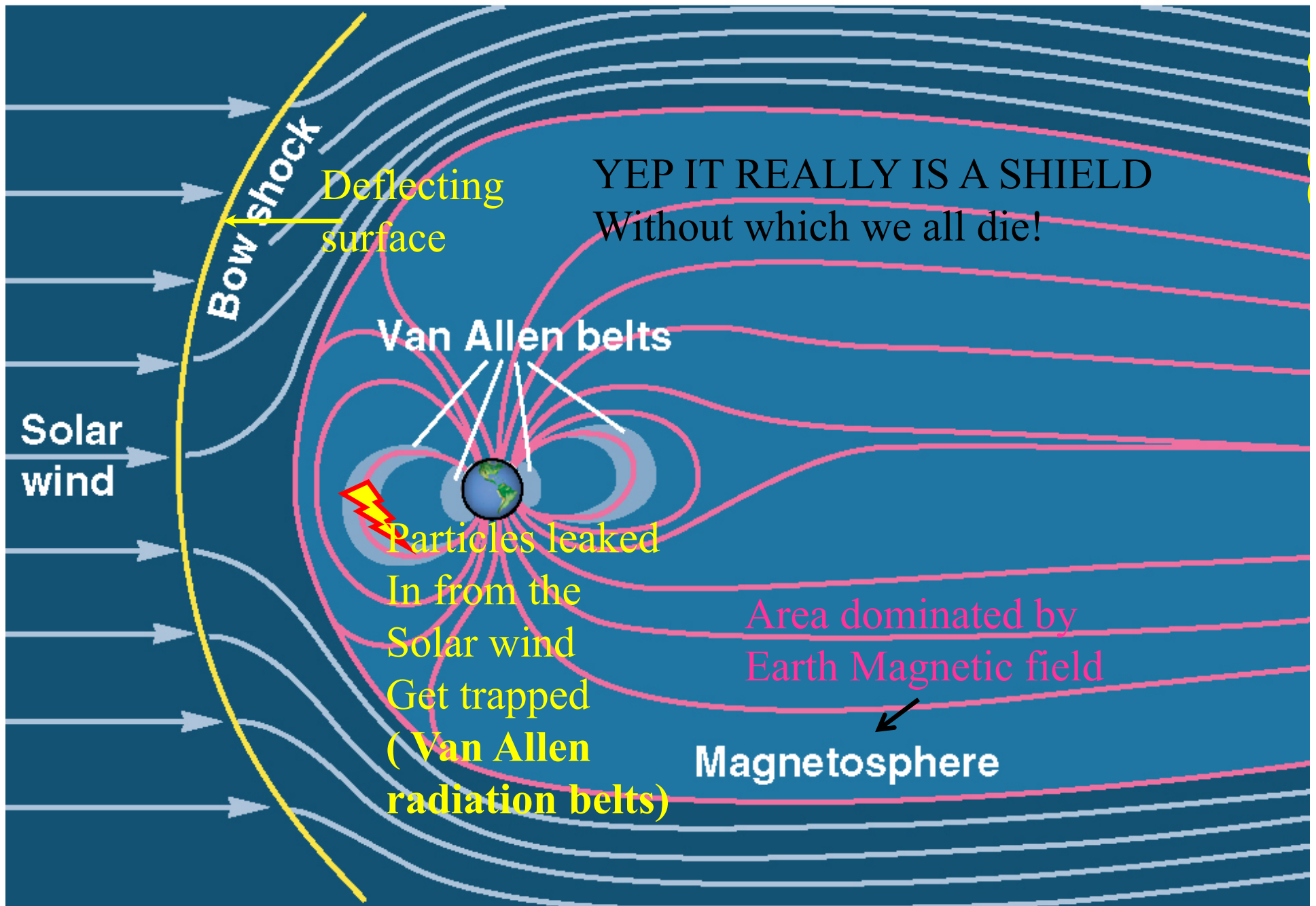
**Earth's MAGNETIC FIELD**

Earth rotates  
Rising heat  
Causes convection  
In liquid core.

Which is a  
Highly electrically  
conductive  
Iron-nickel alloy

**DYNAMO EFFECT**  
=rotation of convecting  
conducting liquid  
generates the  
dipole magnetic field





# AURORA

Solar wind particles  
That leak into the  
Earth's upper  
Atmosphere  
Ionize gas atoms that  
Capture electrons  
Resulting in  
An  
**EMISSION  
SPECTRUM  
Of rays  
& beautiful  
curtains**



# Another Aurora (Polar Light)

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As high-energy particles leak into the lower magnetosphere, they excite molecules near the Earth's magnetic poles, causing the **aurora**

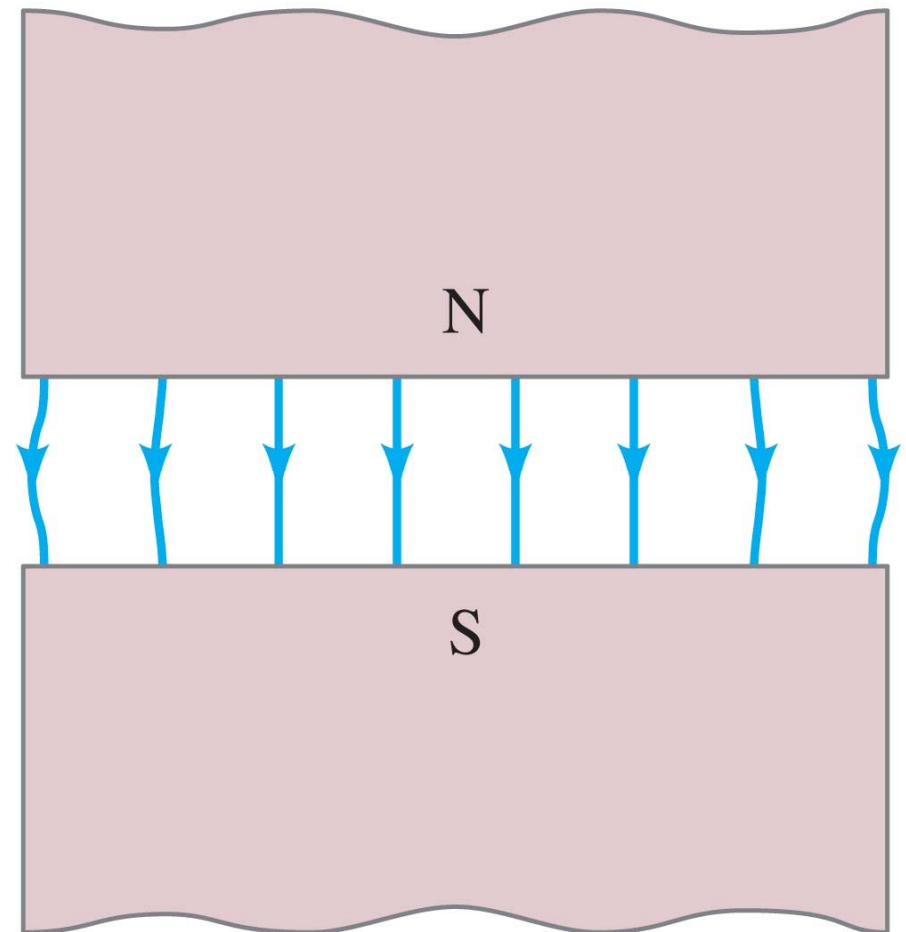
# Aurora are dynamic!

- [Aurora Australis From McMurdo station Antarctica](#)

# 27-1 Magnets and Magnetic Fields

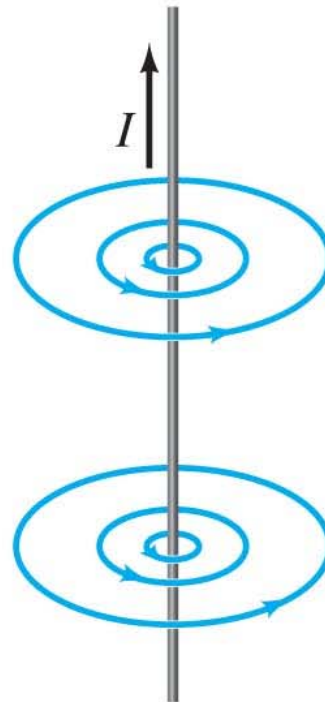
A uniform magnetic field is constant in magnitude and direction.

The field between these two wide poles is nearly uniform.

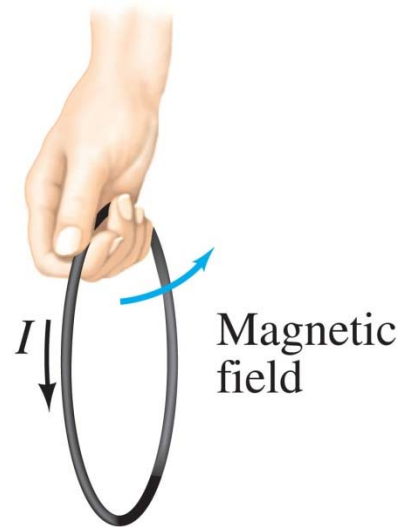
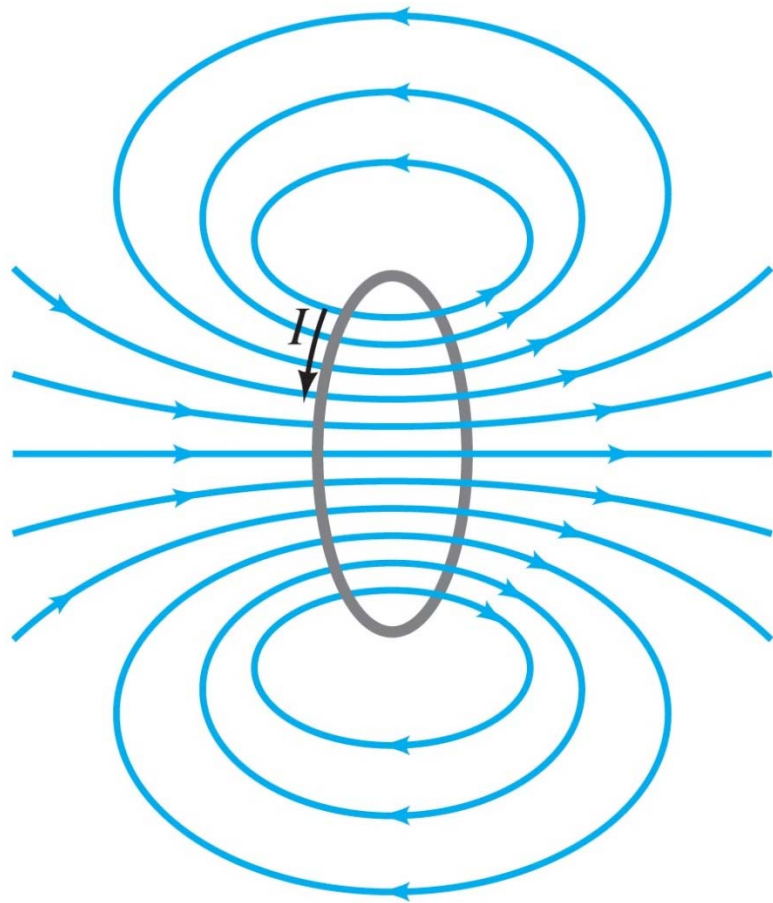


# 27-2 Electric Currents Produce Magnetic Fields

Experiment shows that an electric current produces a magnetic field. The direction of the field is given by a right-hand rule.



# 27-2 Electric Currents Produce Magnetic Fields



Here we see the field due to a current loop; the direction is again given by a right-hand rule.



# 27-3 Force on an Electric Current in a Magnetic Field; Definition of $\vec{B}$

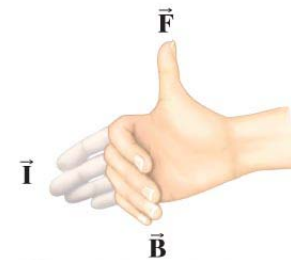
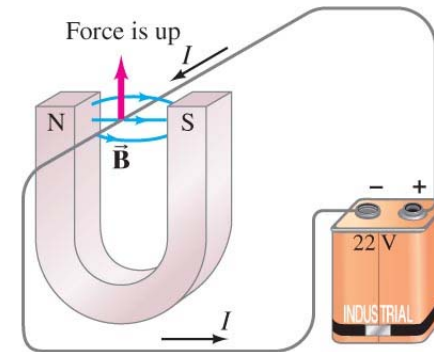
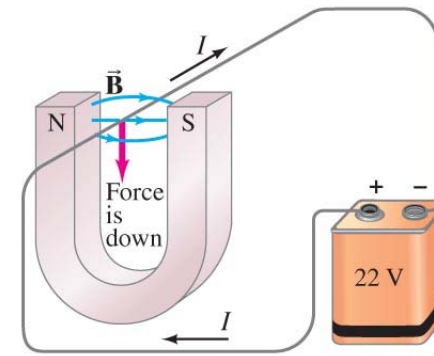
A magnet exerts a force on a current-carrying wire. The direction of the force is given by a right-hand rule.

The force on the wire depends on the current, the length of the wire, the magnetic field, and its orientation:

$$F = I\ell B \sin \theta.$$

$$\vec{F} = I\vec{\ell} \times \vec{B}.$$

This last equation defines the magnetic field in vector notation:



## 27-3 Force on an Electric Current in a Magnetic Field; Definition of $\vec{B}$

Unit of  $B$ : the tesla, T:

$$1 \text{ T} = 1 \text{ N/A}\cdot\text{m. Ie from } F=ilB \rightarrow B=F/il$$

Another unit sometimes used: the gauss (G):

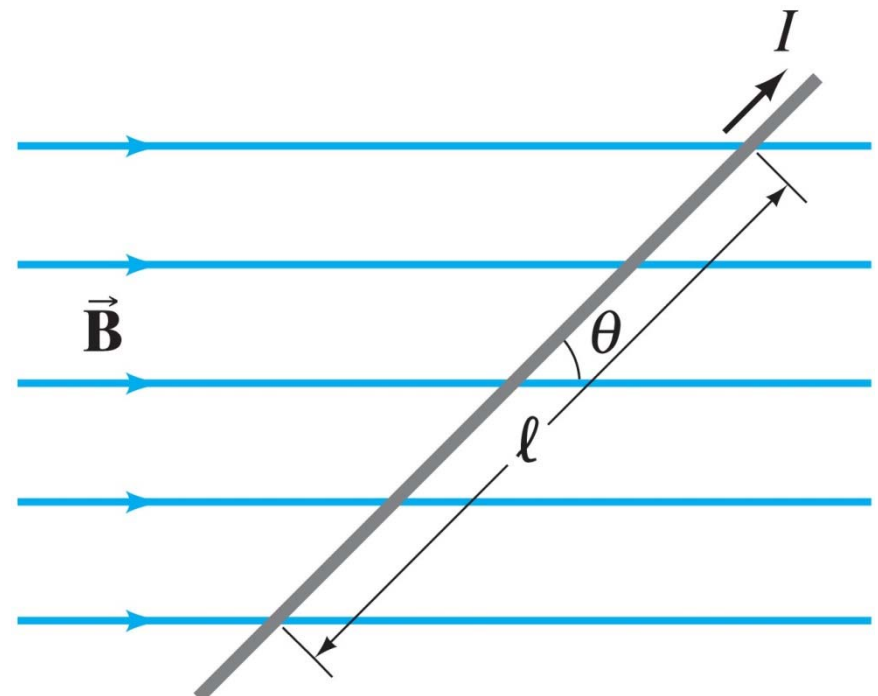
$$1 \text{ G} = 10^{-4} \text{ T.}$$

Earth's field is  $\sim 0.5\text{G}$

## 27-3 Force on an Electric Current in a Magnetic Field; Definition of $\vec{B}$

**Example 27-1: Magnetic Force on a current-carrying wire.**

A wire carrying a 30-A current has a length  $\ell = 12$  cm between the pole faces of a magnet at an angle  $\theta = 60^\circ$ , as shown. The magnetic field is approximately uniform at 0.90 T. We ignore the field beyond the pole pieces. What is the magnitude of the force on the wire?



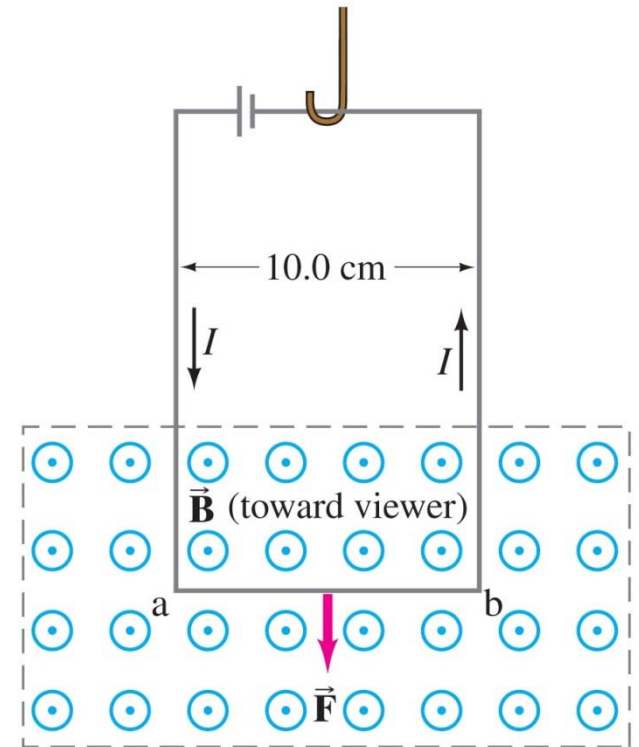
**CLASS**

$$F = I\ell B \sin \theta.$$

# 27-3 Force on an Electric Current in a Magnetic Field; Definition of $\vec{B}$

**Example 27-2: Measuring a magnetic field.**

A rectangular loop of wire hangs vertically as shown. A magnetic field  $\vec{B}$  is directed horizontally, perpendicular to the wire, and points out of the page at all points. The magnetic field is very nearly uniform along the horizontal portion of wire  $ab$  (length  $\ell = 10.0$  cm) which is near the center of the gap of a large magnet producing the field. The top portion of the wire loop is free of the field. The loop hangs from a balance which measures a downward magnetic force (in addition to the gravitational force) of  $F = 3.48 \times 10^{-2}$  N when the wire carries a current  $I = 0.245$  A. What is the magnitude of the magnetic field  $B$ ?



**class**

$$\Theta = 90^\circ \quad F = i\ell B \quad \text{or}$$

$$B = F / i\ell = 1.42 \text{ T}$$

# 27-3 Force on an Electric Current in a Magnetic Field; Definition of $\vec{B}$

## Example 27-3: Magnetic Force on a semicircular wire.

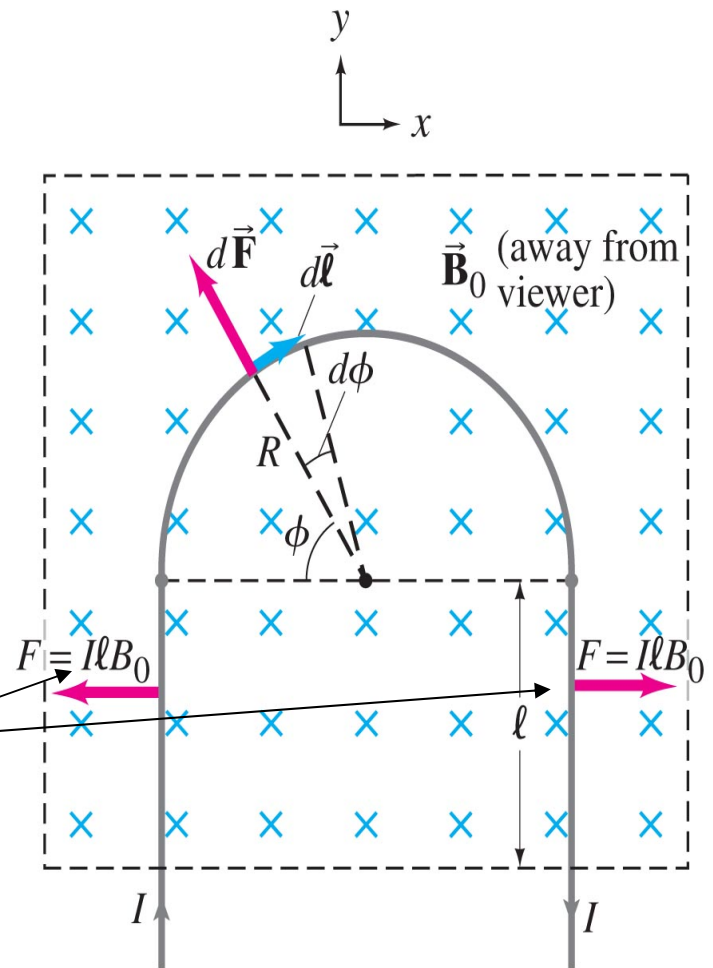
A rigid wire, carrying a current  $I$ , consists of a semicircle of radius  $R$  and two straight portions as shown. The wire lies in a plane perpendicular to a uniform magnetic field  $B_0$ . Note choice  $x$  and  $y$  axis. The straight portions each have length  $\ell$  within the field. Determine the net force on the wire due to the magnetic field.

Note symmetry cancellations all  $x$  Components of  $dF$  and these

Only  $y$  component of  $dF$ ,  $dF \sin \phi$

Also  $dl = R d\phi \rightarrow \sum dF \sin \phi$  &  $dF = i B_0 R d\phi$

$$F = \int_0^\pi dF \sin \phi = I B_0 R \int_0^\pi \sin \phi d\phi = 2 I B_0 R$$



**HAND IN HW. Recall by first Sketch, set up equations, solve algebraically then plug in numbers. All answers in Scientific notation.**

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**85: 27-2**

**86: 27-6**

**87: 27-7**

**88: 27-10**

# 27-4 Force on an Electric Charge Moving in a Magnetic Field

The force on a moving charge is related to the force on a current:

ie. Assume  $i=Q/t=Nq/t$  N number of charges

And v velocity so they travel in t a length  $l=vt$

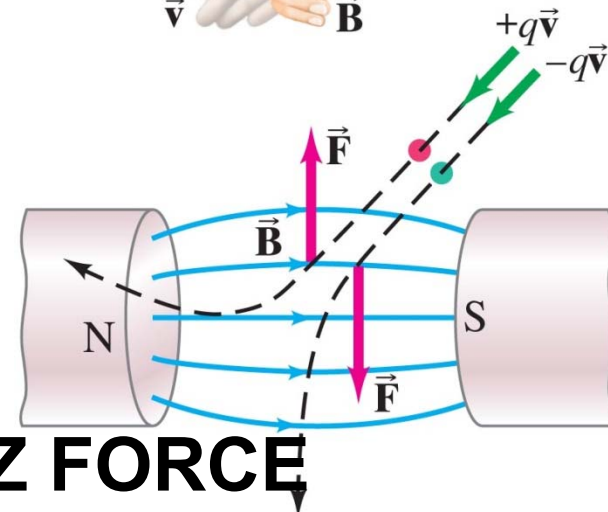
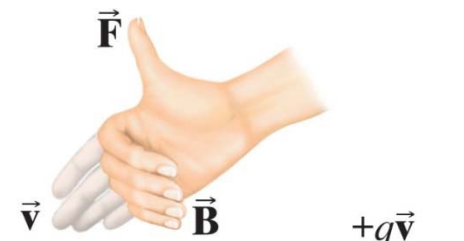
Thus  $F=il \times B=N(q/t)vt \times B = Nqv \times B$   
So for one charge.

$$\vec{F} = q\vec{v} \times \vec{B}.$$

Once again, the direction is given by a right-hand rule.

part of: **THE LORENTZ FORCE**

Right-hand rule



# 27-4 Force on an Electric Charge Moving in a Magnetic Field

**Conceptual Example 27-4: Negative charge near a magnet.**

**A negative charge  $-Q$  is placed at rest near a magnet. Will the charge begin to move? Will it feel a force? What if the charge were positive,  $+Q$ ?**

**CLASS?**



# 27-4 Force on an Electric Charge Moving in a Magnetic Field

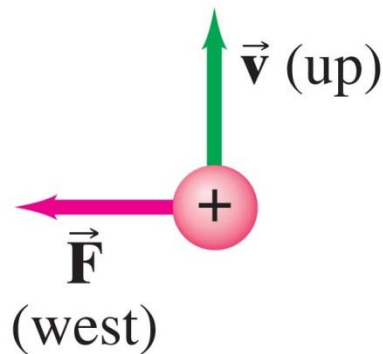
**Example 27-5: Magnetic force on a proton.**

A magnetic field exerts a force of  $8.0 \times 10^{-14}$  N toward the west on a proton moving vertically upward at a speed of  $5.0 \times 10^6$  m/s. When moving horizontally in a northerly direction, the force on the proton is zero. Determine the magnitude and direction of the magnetic field in this region. (The charge on a proton is  $q = +e = 1.6 \times 10^{-19}$  C.)

**Direction of B?**

**Angle  $\theta$  ?**

$$B = F/qv = 0.1 \text{ T}$$



# 27-4 Force on an Electric Charge Moving in a Magnetic Field

**Example 27-6: Magnetic force on ions during a nerve pulse.**

**Estimate the magnetic force due to the Earth's magnetic field on ions crossing a cell membrane during an action potential. Assume the speed of the ions is  $10^{-2}$  m/s.  $B \sim 0.5$  G  $\sim 10^{-4}$  T**

$$F \sim qvB \sim 10^{-19} \text{C} \cdot 10^{-2} \text{ m/s} \times 10^{-4} \text{T} = 10^{-25} \text{N}$$

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**89: 27- 13**

**90: 27- 14**

**91: 27- 16**

# 27-4 Force on an Electric Charge Moving in a Magnetic Field

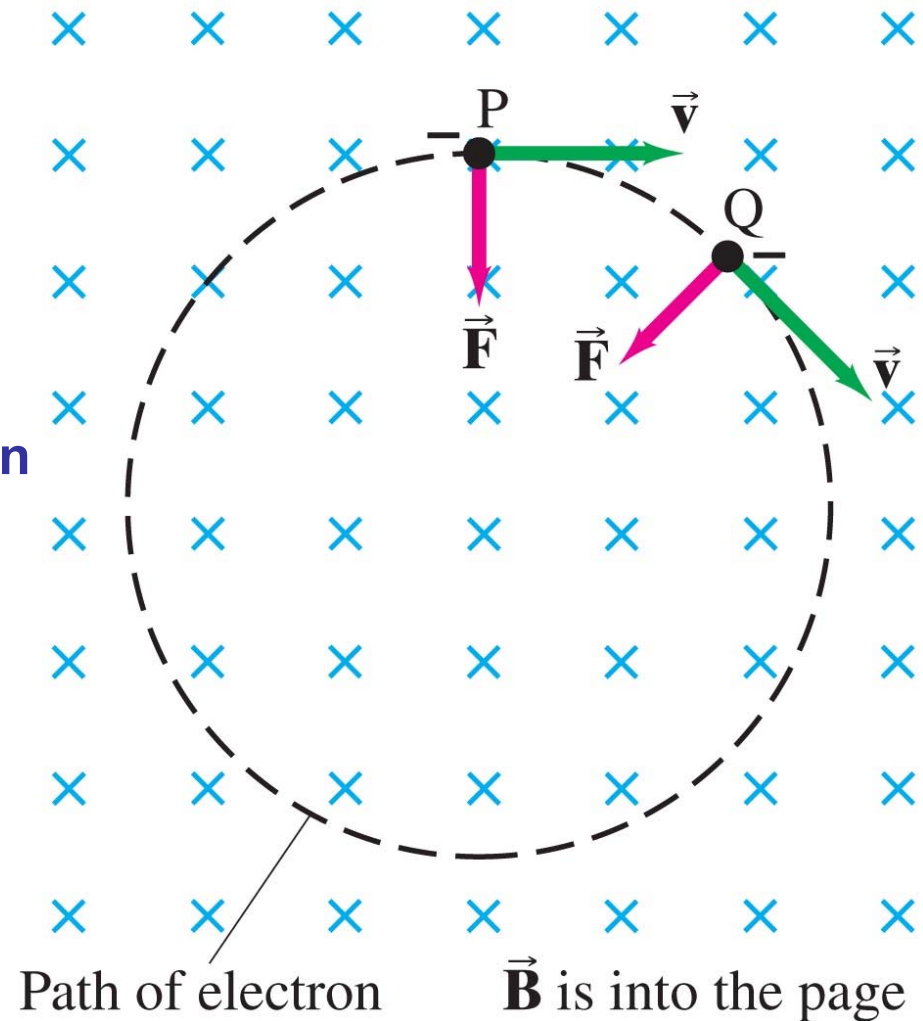
If a charged particle is moving **perpendicular** to a uniform magnetic field, its path will be a circle. **NOTE Perpendicular!!!**

**Example 27-7: Electron's path in a uniform magnetic field.**

An electron travels at  $2.0 \times 10^7$  m/s in a plane perpendicular to a uniform 0.010-T magnetic field. Describe its path quantitatively.

the radius of path, period and Frequency of orbit

**CLASS?**



# 27-4 Force on an Electric Charge Moving in a Magnetic Field

Given:  $v=2.0 \times 10^7 \text{ m/s}$   $B=0.010\text{T}$

radius of path, period and frequency of orbit ?

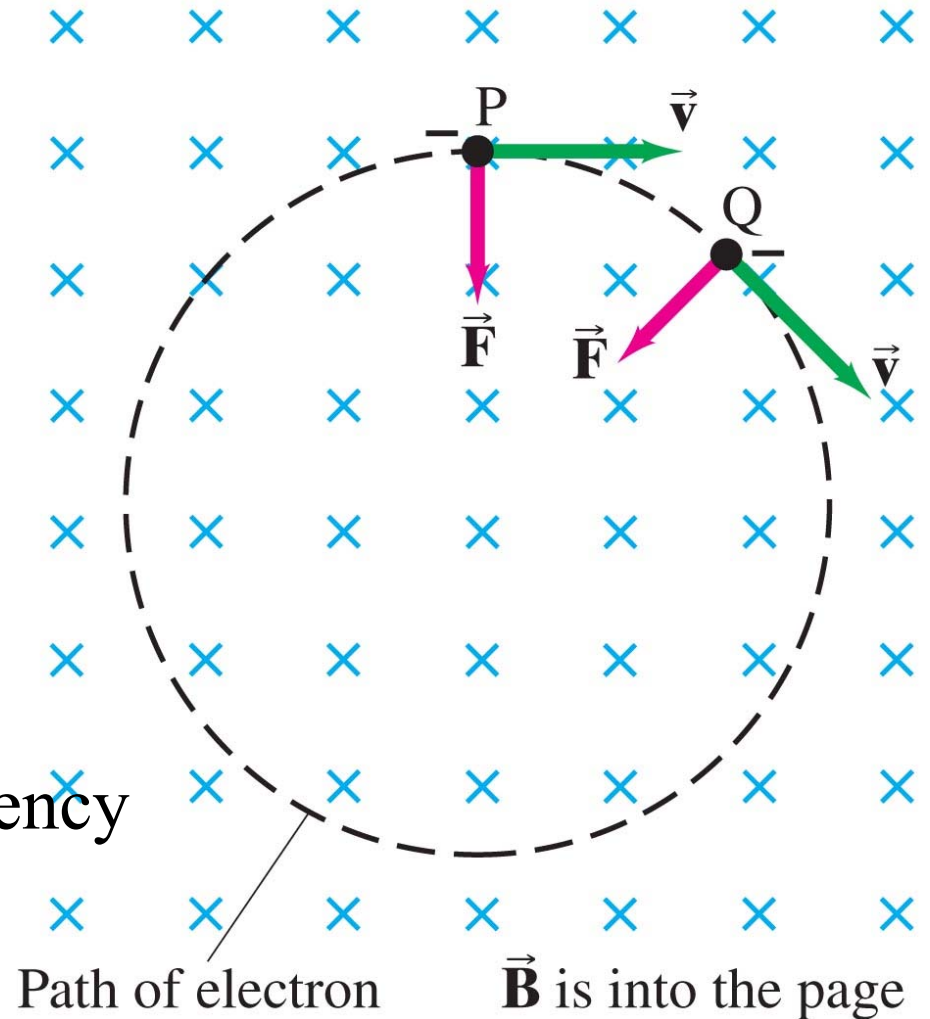
$$\Sigma F=ma \rightarrow \text{so } qvB=mv^2 / r$$

$$r=mv/qB \text{ (v, B, \& r constant!)}$$

$$T=2\pi r/v = 2\pi r/qBr/m =$$

$$2\pi m/qB$$

$$f = qB/2\pi m \rightarrow \text{Cyclotron frequency}$$



# **27-4 Force on an Electric Charge Moving in a Magnetic Field**

**Conceptual Example 27-8: Stopping charged particles.**

**Can a magnetic field be used to stop a single charged particle, as an electric field can?**

**CLASS**


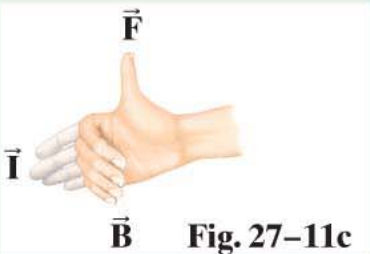
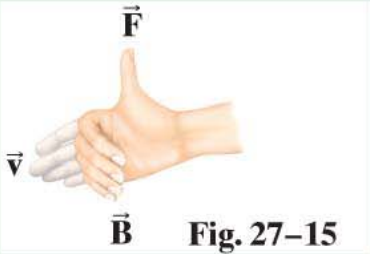
# **27-4 Force on an Electric Charge Moving in a Magnetic Field**

**Problem solving: Magnetic fields – things to remember:**

- 1. The magnetic force is perpendicular to the magnetic field direction.**
- 2. The right-hand rule is useful for determining directions.**
- 3. Equations in this chapter give magnitudes only. The right-hand rule gives the direction.**

# 27-4 Force on an Electric Charge Moving in a Magnetic Field

**TABLE 27-1 Summary of Right-hand Rules (= RHR)**

Physical Situation	Example	How to Orient Right Hand	Result
1. Magnetic field produced by current (RHR-1)	 <p>Fig. 27-8c</p>	Wrap fingers around wire with thumb pointing in direction of current $I$	Fingers point in direction of $\vec{B}$
2. Force on electric current $I$ due to magnetic field (RHR-2)	 <p>Fig. 27-11c</p>	Fingers point straight along current $I$ , then bend along magnetic field $\vec{B}$	Thumb points in direction of the force $\vec{F}$
3. Force on electric charge $+q$ due to magnetic field (RHR-3)	 <p>Fig. 27-15</p>	Fingers point along particle's velocity $\vec{v}$ , then along $\vec{B}$	Thumb points in direction of the force $\vec{F}$



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**92: 27 - 15**

**93: 27 - 18**

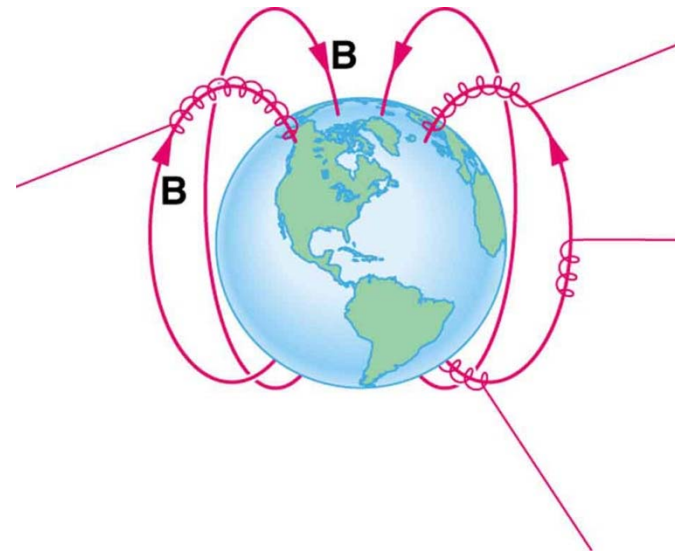
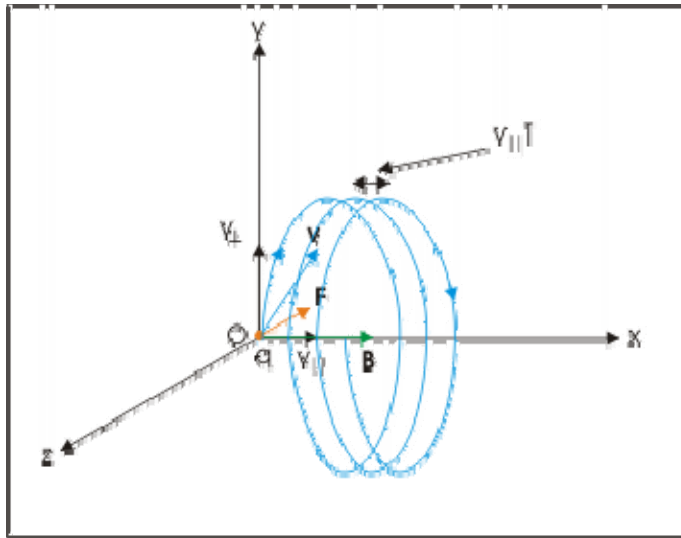
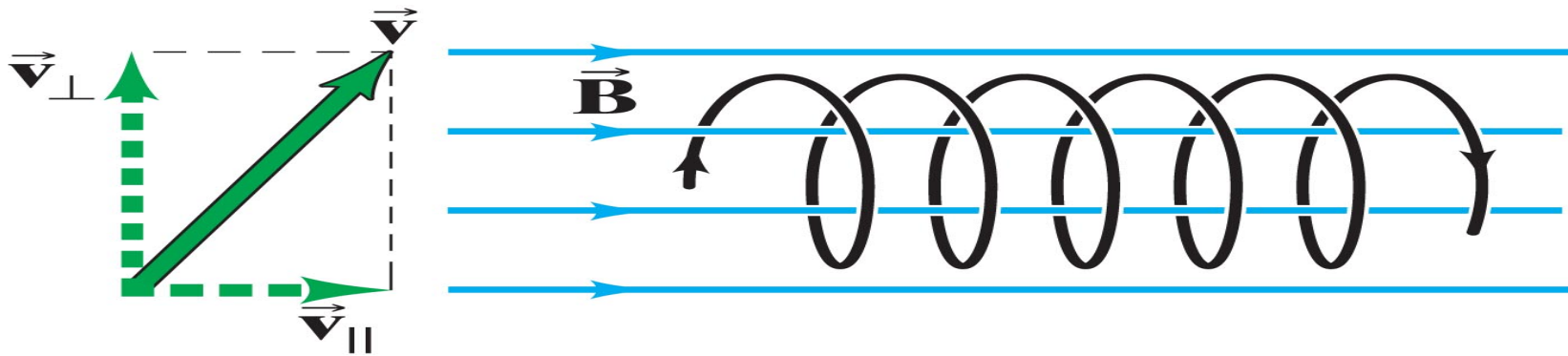
**94: 27- 19**

**95: 27- 22**

## 27-4 Force on an Electric Charge Moving in a Magnetic Field

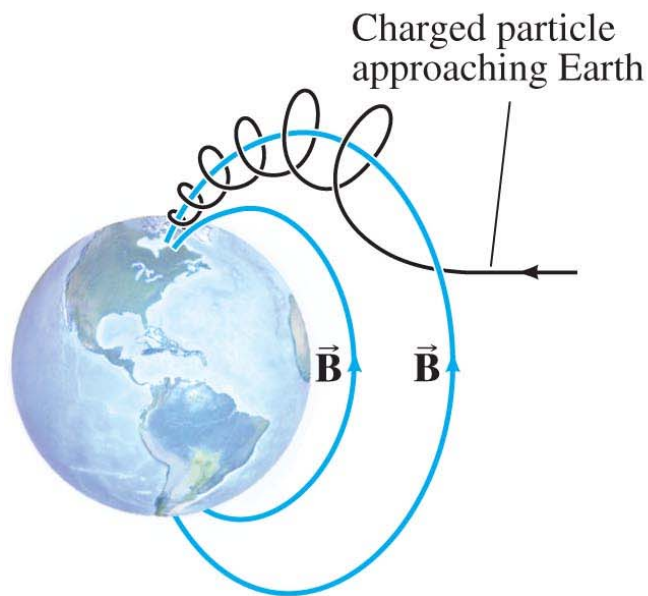
### Conceptual Example 27-9: A helical path.

What is the path of a charged particle in a uniform magnetic field if its velocity is not perpendicular to the magnetic field?



# 27-4 Force on an Electric Charge Moving in a Magnetic Field

The aurora borealis (northern lights) is caused by charged particles from the solar wind spiraling along the Earth's magnetic field, and colliding with air molecules.



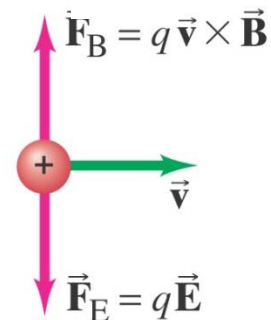
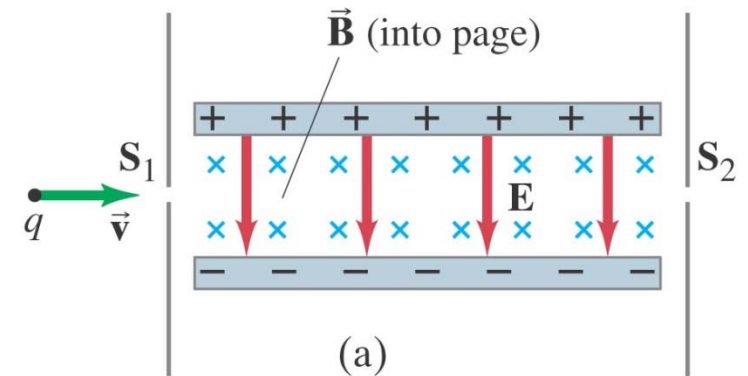
# 27-4 Force on an Electric Charge Moving in a Magnetic Field

Conceptual Example 27-10:

**Velocity selector**, or filter: crossed  $\vec{E}$  and  $\vec{B}$  fields.

Some electronic devices and experiments need a beam of charged particles all moving at nearly the same velocity. This can be achieved using both a uniform electric field and a uniform magnetic field, arranged so they are at right angles to each other. Particles of charge  $q$  pass through slit  $S_1$  and enter the region where  $\vec{B}$  points into the page and  $\vec{E}$  points down from the positive plate toward the negative plate. If the particles enter with different velocities, show how this device “selects” a particular velocity, and determine what this velocity is.

**CLASS?**



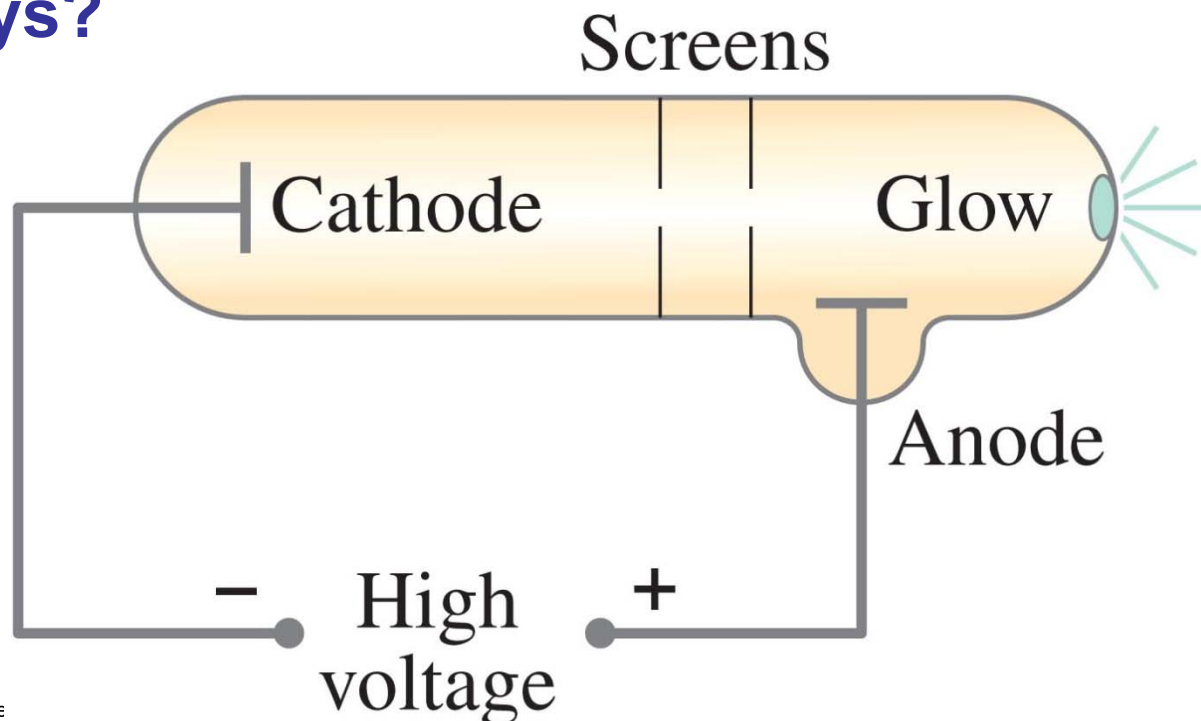
$$\Sigma \mathbf{F} = \mathbf{0}$$

$$q\mathbf{v}\mathbf{B} = q\mathbf{E} \text{ get thru!}$$

$$\text{Only! } \mathbf{v} = \mathbf{E}/\mathbf{B}!$$

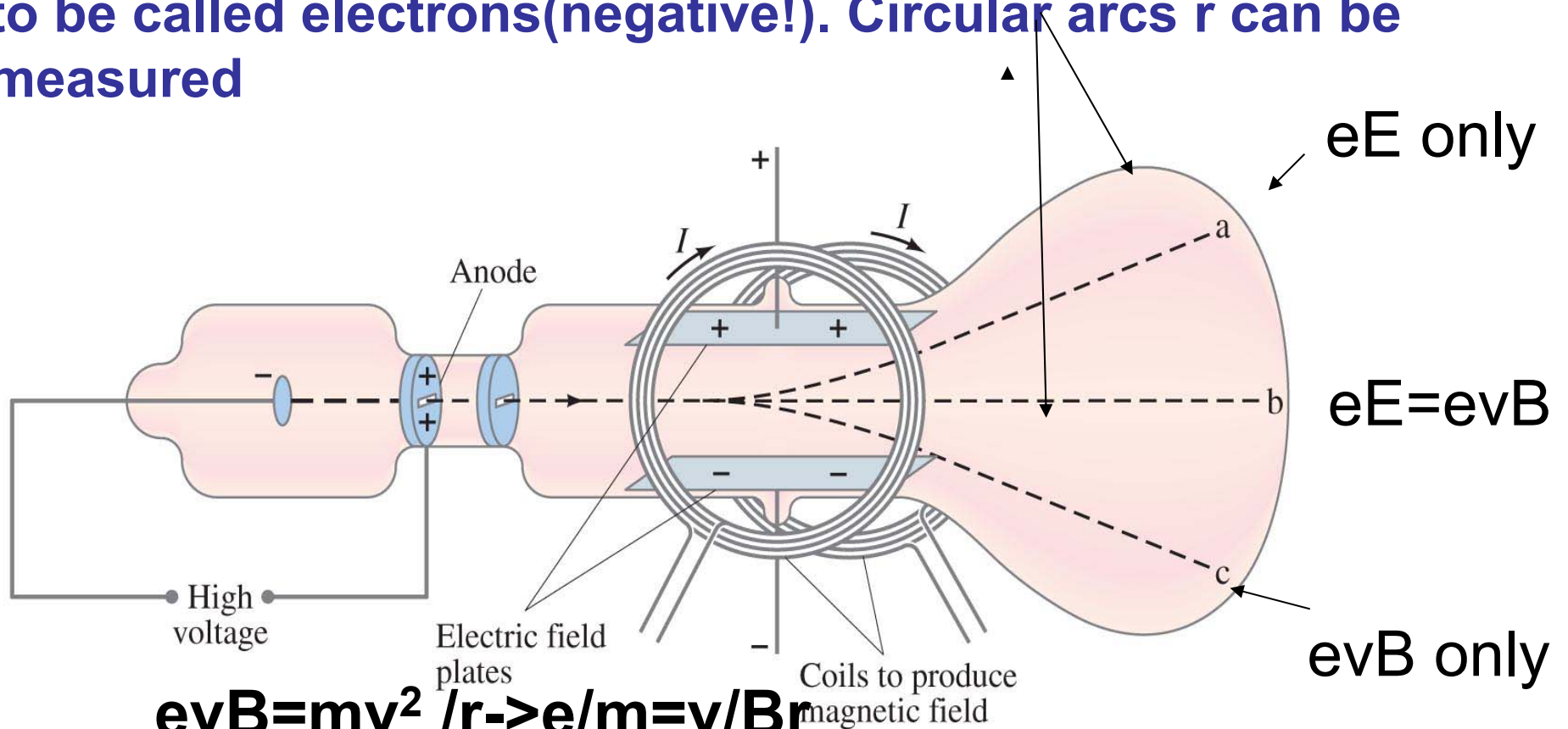
# 27-7 Discovery and Properties of the Electron

Electrons were first observed in cathode ray tubes. These tubes had a very small amount of gas inside, and when a high voltage was applied to the cathode, some “cathode rays” appeared to travel from the cathode to the anode. What are these mysterious rays?



# 27-7 Discovery and Properties of the Electron

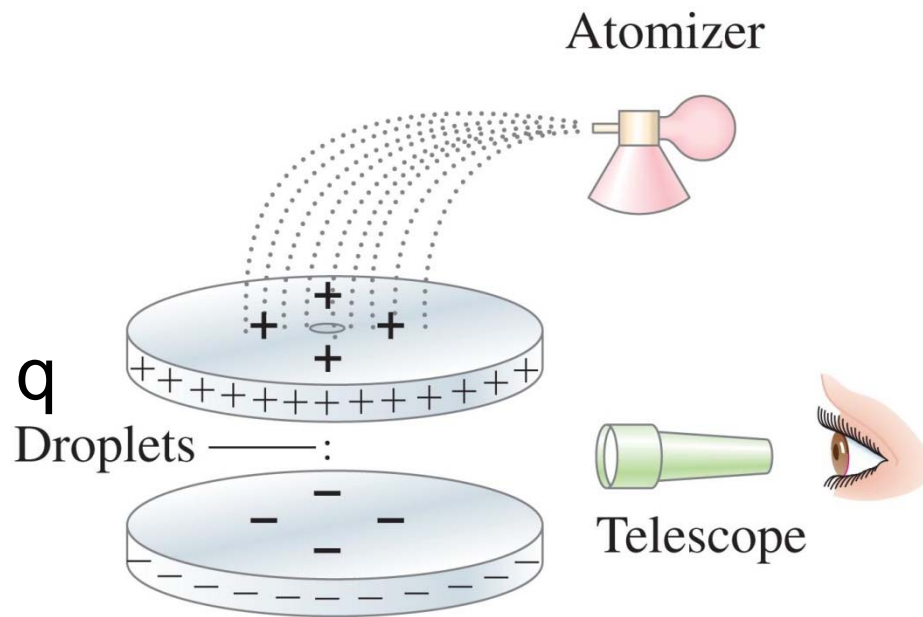
The value of  $e/m$  for the cathode rays was measured in 1897 using the apparatus below; it was then that the rays began to be called electrons (negative!). Circular arcs  $r$  can be measured



Find  $v$ ? with point  $b$   $v = E/B$  so  $e/m = E/B^2 r$

# 27-7 Discovery and Properties of the Electron

Millikan measured the electron charge directly shortly thereafter, using the oil-drop apparatus diagrammed below, and showed that the electron was a constituent of the atom (and not an atom itself, as its mass is far too small).



$qE=mg$  balance drops  
 $q=mg/E$   $m$  is found by  
A different technique

Experiment yields  
 $Q=Ne!$

The currently accepted values of  
the electron mass and charge are

$$m = 9.1 \times 10^{-31} \text{ kg}$$

$$e = 1.6 \times 10^{-19} \text{ C}$$

# 27-9 Mass Spectrometer

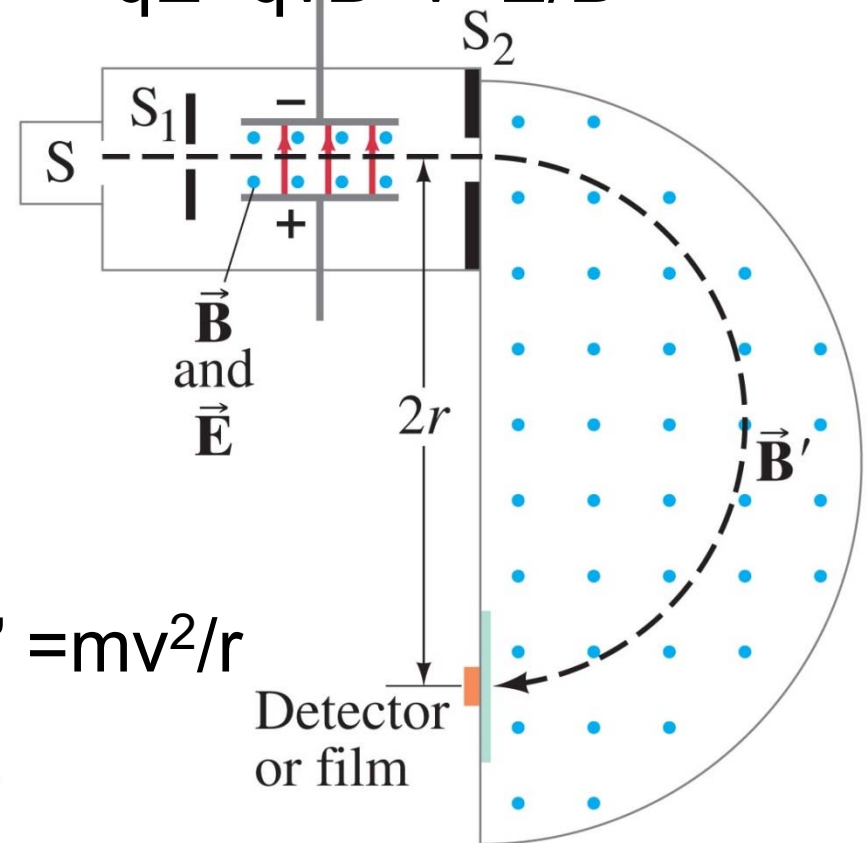
A mass spectrometer measures the masses of atoms. If a charged particle is moving through perpendicular electric and magnetic fields, there is a particular speed at which it will not be deflected, which then allows the measurement of its mass:

All the atoms reaching the second magnetic field will have the same speed; their radius of curvature will depend on their mass.

$$m = \frac{qB'r}{v} = \frac{qBB'r}{E}$$

**Vel. select**

$$qE = qvB \quad v = E/B$$



$$qvB' = mv^2/r$$

**If all fields are known we measure r and get m  
two or more r's from sample S = isotopes**



# 27-9 Mass Spectrometer

**Example 27-14: Mass spectrometry.**

**Carbon atoms of atomic mass 12.0 u are found to be mixed with another, unknown, element. In a mass spectrometer with fixed  $B'$ , the carbon traverses a path of radius 22.4 cm and the unknown's path has a 26.2-cm radius. What is the unknown element? Assume the ions of both elements have the same charge.**

**CLASS?**

$$m_x/m_C = r_x/r_C = 1.17 \quad m_x = 1.17m_C = 14.0u$$



**HAND IN HW. Recall by first Sketch, set up equations, solve algebraically then plug in numbers. All answers in Scientific notation.**

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**96: 27-20**

**97: 27- 22**

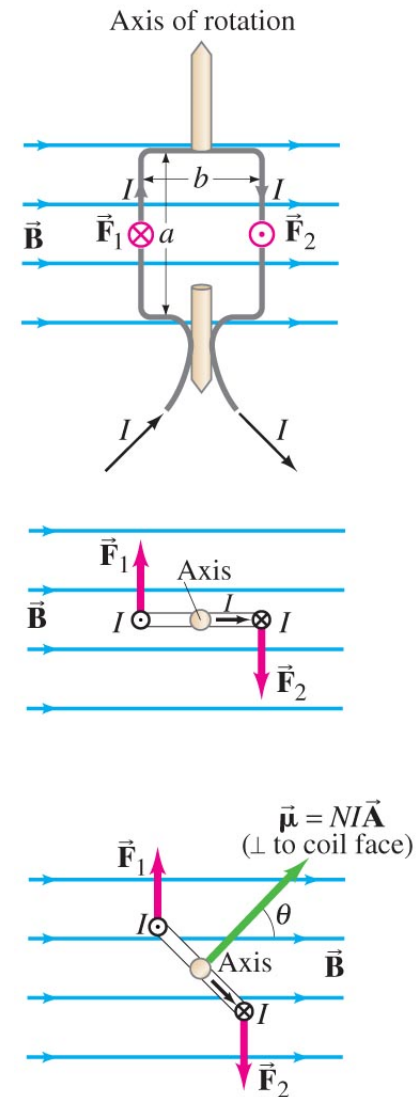
**98: 27-25**

# 27-5 Torque on a Current Loop; Magnetic Dipole Moment

The forces on opposite sides of a current loop will be equal and opposite (if the field is uniform and the loop is symmetric), but there may be a torque.

The magnitude of the torque is given by

$$\tau = NIAB \sin \theta.$$



# 27-5 Torque on a Current Loop; Magnetic Dipole Moment

The quantity  $NIA$  is called the magnetic dipole moment,  $\mu$ :

$$\vec{\mu} = NI\vec{A}.$$

The potential energy of the loop depends on its orientation in the field:

$$U = -\mu B \cos \theta = -\vec{\mu} \cdot \vec{B}.$$

# **27-5 Torque on a Current Loop; Magnetic Dipole Moment**

**Example 27-11: Torque on a coil.**

**A circular coil of wire has a diameter of 20.0 cm and contains 10 loops. The current in each loop is 3.00 A, and the coil is placed in a 2.00-T external magnetic field. Determine the maximum and minimum torque exerted on the coil by the field.**

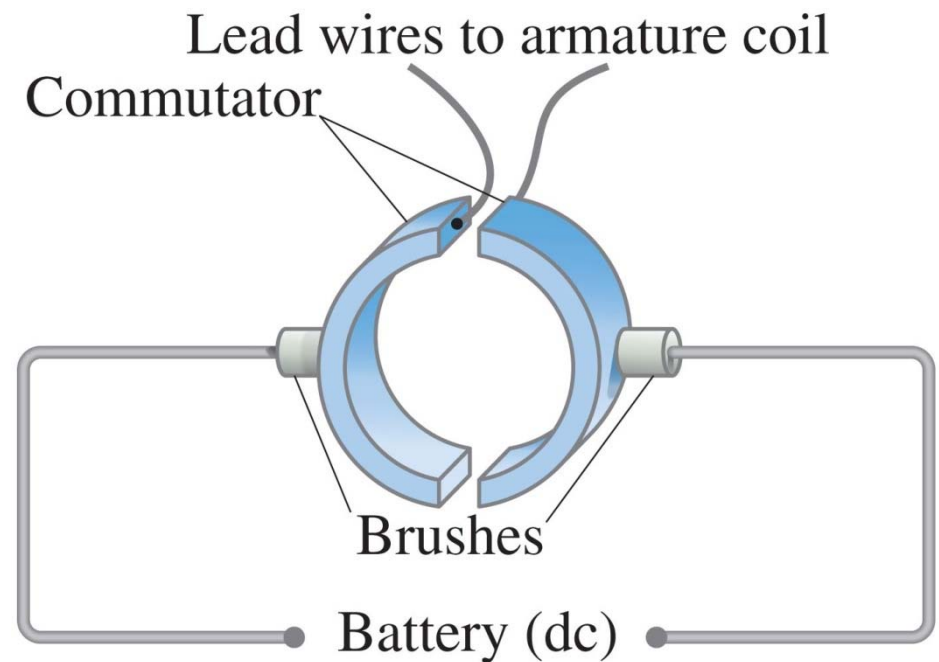
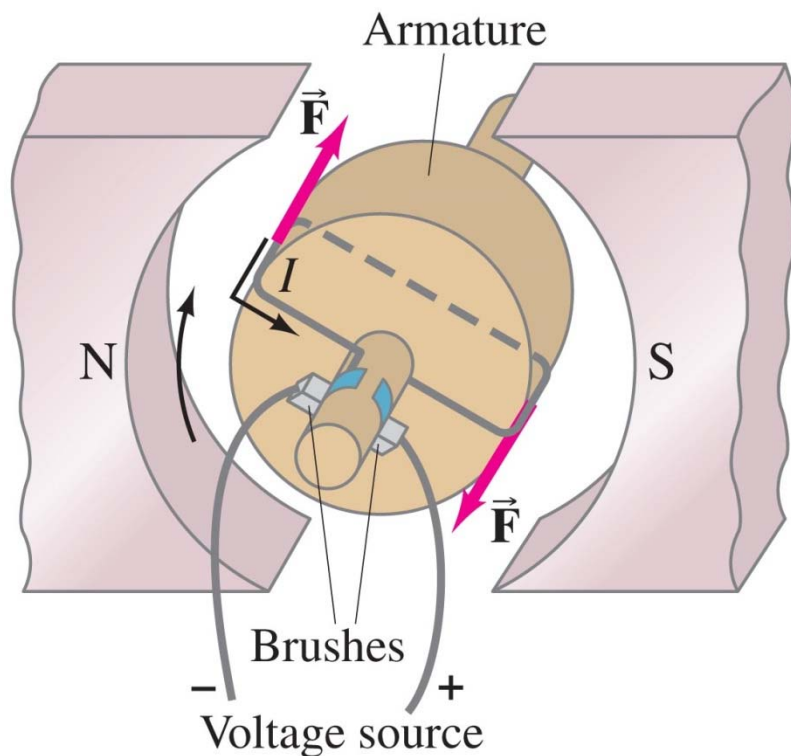
# 27-5 Torque on a Current Loop; Magnetic Dipole Moment

**Example 27-12: Magnetic moment of a hydrogen atom.**

**Determine the magnetic dipole moment of the electron orbiting the proton of a hydrogen atom at a given instant, assuming (in the Bohr model) it is in its ground state with a circular orbit of radius  $r = 0.529 \times 10^{-10}$  m. [This is a very rough picture of atomic structure, but nonetheless gives an accurate result.]**

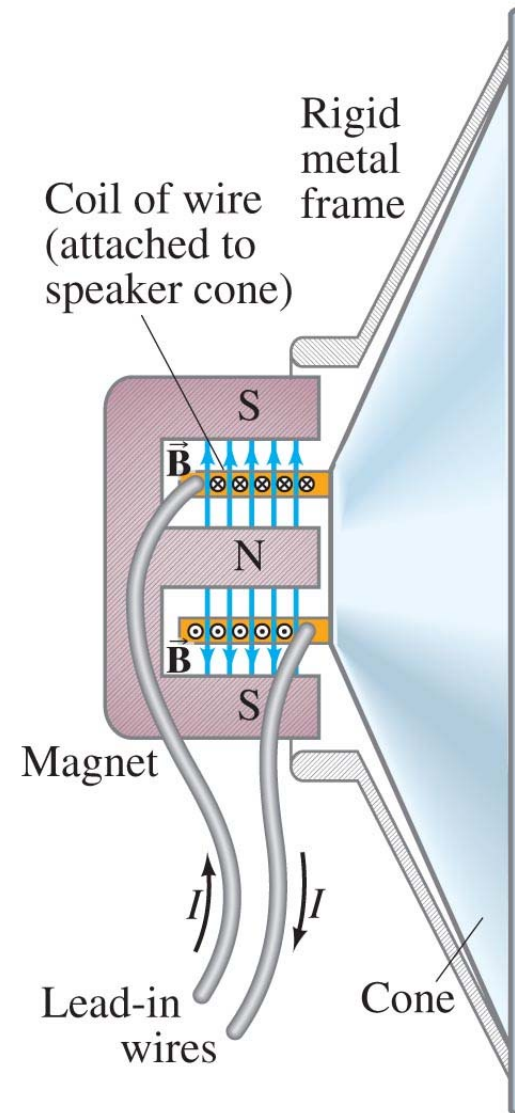
# 27-6 Applications: Motors, Loudspeakers, Galvanometers

An electric motor uses the torque on a current loop in a magnetic field to turn magnetic energy into kinetic energy.



# 27-6 Applications: Motors, Loudspeakers, Galvanometers

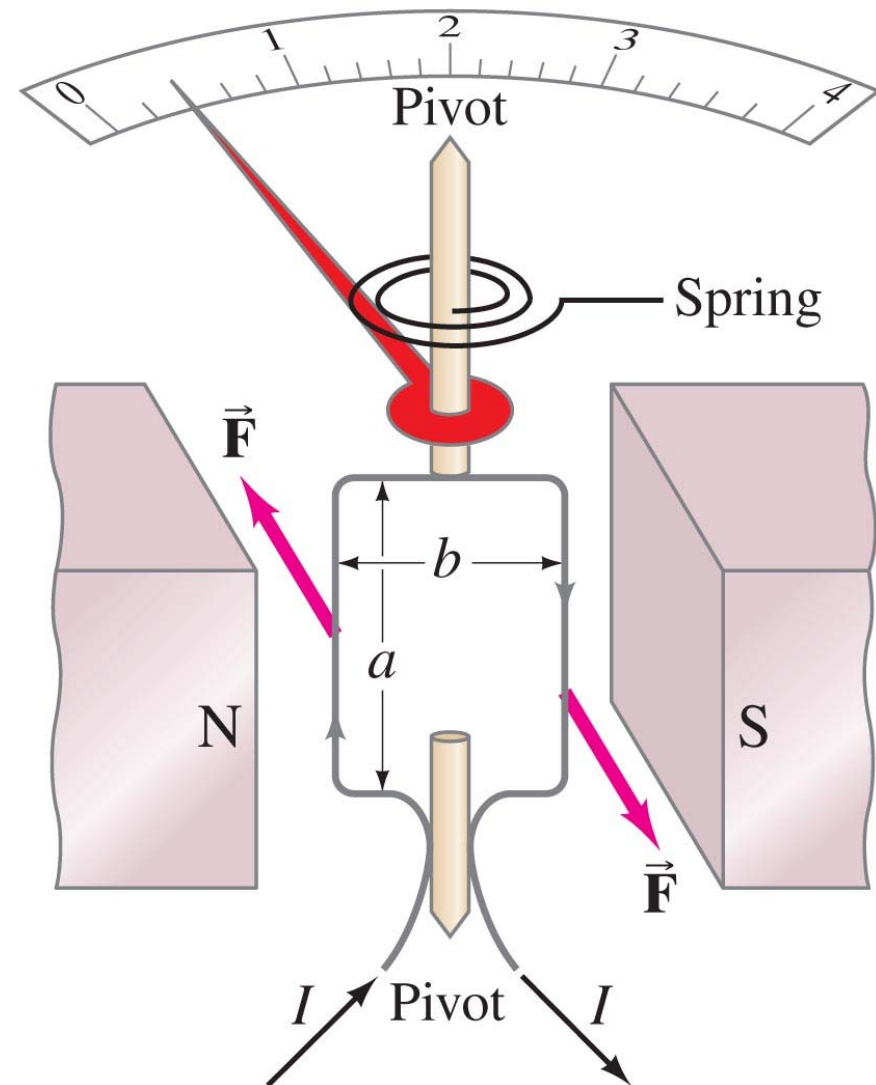
Loudspeakers use the principle that a magnet exerts a force on a current-carrying wire to convert electrical signals into mechanical vibrations, producing sound.





## 27-6 Applications: Motors, Loudspeakers, Galvanometers

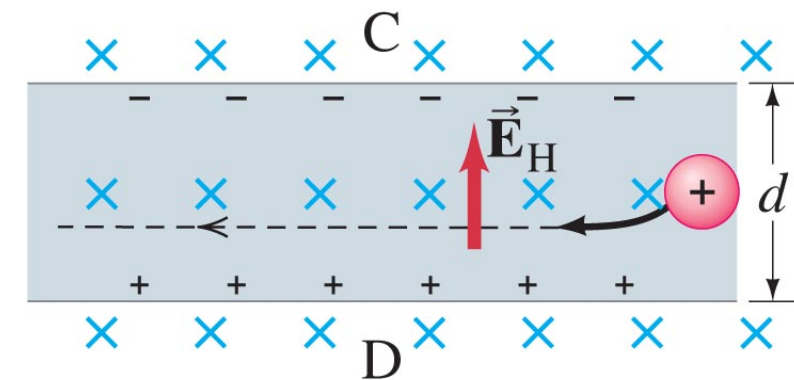
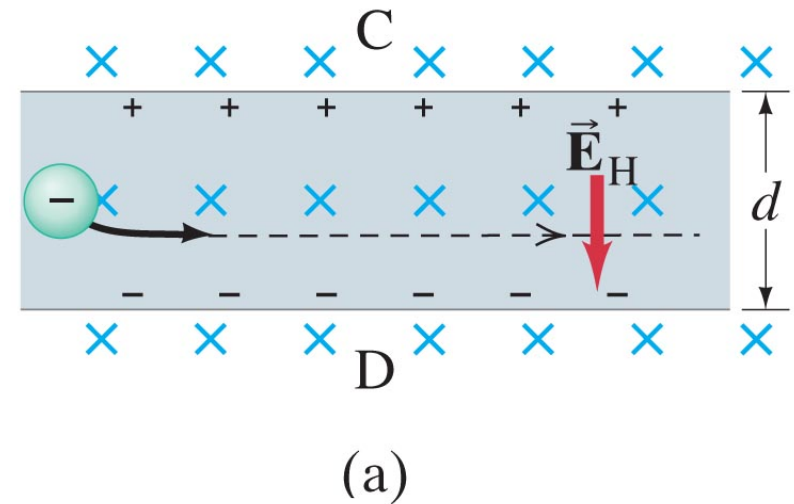
A galvanometer takes advantage of the torque on a current loop to measure current; the spring constant is calibrated so the scale reads in amperes.



**SKIP WHAT FOLLOWS SPR 16**

## 27-8 The Hall Effect->Hall Probe to measure magnetic fields

When a current-carrying wire is placed in a magnetic field, there is a sideways force on the electrons in the wire. This tends to push them to one side and results in a potential difference from one side of the wire to the other; this is called the Hall effect. The emf differs in sign depending on the sign of the charge carriers; this is how it was first determined that the charge carriers in ordinary conductors are negatively charged.



$$\Sigma F=0 \rightarrow eE_H = ev_d B$$

$$EMF(V) = E_H d = v_d B d$$

## 27-8 The Hall Effect

**Example 27-13: Drift velocity using the Hall effect.**

A long copper strip 1.8 cm wide and 1.0 mm thick is placed in a 1.2-T magnetic field. When a steady current of 15 A passes through it, the Hall emf is measured to be  $1.02 \mu\text{V}$ . Determine the drift velocity of the electrons and the density of free (conducting) electrons (number per unit volume) in the copper.

